

Table 1: Notation Standard for *Planetary Ring Systems*

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The following variables have changed since the draft of October 23:  $B$ ,  $B_{\odot}$ ,  $D_2$ ,  $D_3$ ,  $D_e$ ,  $I/F$ ,  $N_2$ ,  $N_3$ ,  $Q$ ,  $Q_{\text{ext}}$ ,  $Q_{\text{T}}$ ,  $R$ ,  $W$ ,  $W_e$ ,  $s$ ,  $\alpha$ ,  $\kappa$ ,  $\mu$ ,  $\mu_0$ ,  $\nu$ ,  $\dot{\Omega}$ ,  $\varpi_0$ ,  $\dot{\varpi}$ ,  $\tau_{\text{LOS}}$ ,  $\tau_{\perp}$

$B$	elevation angle (angle of observer above rings): $B =  90^{\circ} - \theta_e $
$B_{\odot}$	solar elevation angle (angle of Sun above rings): $B_{\odot} =  90^{\circ} - \theta_i $
$D_2$	area filling factor (fraction of ring surface area occupied by particles)
$D_3$	volume filling factor (fraction of total volume occupied by particles)
$D_e$	equivalent depth (see Glossary)
$E$	Orbital energy
$F_D$	azimuthal drag force
$F_G$	central gravitational force from planet, $GM_P m/a^2$
$F_I$	inertially fixed force
$F_m$	gravitational force from a moon
$F_N$	component of perturbing force normal to orbit plane
$F_r$	radial component of perturbing force (cylindrical coordinates)
$F_R$	radial component of perturbing force (spherical coordinates)
$F_z$	vertical component of perturbing force
$F_{\lambda}$	azimuthal component of perturbing force
$F_{\Theta}$	tangential component of perturbing force (in orbit plane)
$G$	gravitational constant
$H$	ring vertical thickness
$I$	orbital inclination
$I/F$	reflectivity (see Glossary)
$I_m$	moon's inclination
$J_2$	planetary oblateness parameter
$\vec{L}$	orbital angular momentum
$M_P$	planet mass
$M_m$	moon mass
$N_2$	surface number density of ring particles
$N_3$	volume number density of ring particles
$Q$	tidal quality factor
$Q_{\text{ext}}$	photometric extinction coefficient

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$Q_T$	Toomre's $Q$
$R$	physical radius of an object
$U$	gravitational potential
$V_r$	average radial velocity of ring particles
$V_z$	average vertical velocity of ring particles
$V_\lambda$	average azimuthal velocity of ring particles
$W$	radial width
$W_e$	equivalent width (see Glossary)
$a$	orbital semi-major axis
$a_m$	moon's orbital semi-major axis
$c$	root-mean-square ( <i>rms</i> ) velocity dispersion
$c_z$	vertical <i>rms</i> velocity dispersion
$e$	orbital eccentricity
$e_f$	forced eccentricity
$e_l$	free eccentricity
$e_m$	moon's eccentricity
$f$	true anomaly
$h$	$e \cos(\varpi - \lambda_0)$
$k$	$e \sin(\varpi - \lambda_0)$
$k_r$	radial wavenumber
$m$	ring particle mass
$n$	orbital mean motion
$n_P$	pattern speed
$r_H$	Hill radius
$r_R$	Roche limit
$\vec{r}$	particle's position vector
$r$	radial distance from planet's spin axis
$s$	ring particle radius (in context of a size distribution)
$u_r$	random radial velocity of ring particles
$u_z$	random vertical velocity of ring particles
$u_\lambda$	random azimuthal velocity of ring particles
$\vec{v}$	particle's velocity vector
$v_r$	radial velocity of ring particles
$v_z$	vertical velocity of ring particles
$v_\lambda$	azimuthal velocity of ring particles
$x$	cartesian approximation of radial coordinate

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$y$	cartesian approximation of azimuthal coordinate
$z$	vertical displacement above ring-plane
$\alpha$	phase angle
$\epsilon$	coefficient of restitution
$\kappa$	radial (epicyclic) frequency
$\lambda$	inertial longitude
$\lambda_0$	reference longitude
$\lambda_T$	Toomre critical wavelength
$\mu$	$\sin B$
$\mu_0$	$\sin B_\odot$
$\nu$	vertical frequency
$\nu_{\text{eff}}$	effective kinematic shear viscosity
$\Omega$	longitude of ascending node
$\Omega_m$	moon's longitude of ascending node
$\dot{\Omega}$	nodal regression rate
$\dot{\Omega}_0$	free nodal regression rate
$\omega$	argument of pericenter
$\omega_c$	collision frequency
$\varpi$	longitude of pericenter
$\varpi_0$	single-scattering albedo
$\varpi_m$	moon's longitude of pericenter
$\dot{\varpi}$	apsidal precession rate
$\dot{\varpi}_0$	free apsidal precession rate
$\varphi_{CR}$	resonant argument of a corotation resonance
$\varphi_{LR}$	resonant argument of a Lindblad resonance
$\varphi_{VR}$	resonant argument of a vertical resonance
$\rho$	ring particle mass density
$\rho_{\text{crit}}$	Roche critical density
$\rho_P$	planet mass density
$\Sigma$	ring surface mass density
$\tau$	ring optical depth
$\tau_D$	dynamical optical depth
$\tau_{\text{LOS}}$	line-of-sight optical depth
$\tau_\perp$	normal optical depth
$\theta_e$	emission angle (angle of target-observer vector from north pole)

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$\theta_i$	incidence angle (angle of target-Sun vector from north pole)
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